

1 **Mixed convection heat transfer of turbulent flow in a three-**
2 **dimensional lid-driven cavity with a rotating cylinder**
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7 **Abstract**

8 *A numerical study has been carried out to investigate the combined forced and natural*
9 *convection heat transfer in a differentially heated 3D obstructed cavity with a thermally*
10 *insulated rotating circular cylinder. The cavity has a hot stationary bottom wall and a cold top*
11 *lid-driven wall, and all the other walls completing the domain are motionless and adiabatic.*
12 *The simulations are performed for different Reynolds numbers, $Re = 5000, 10000, 15000$ and*
13 *30000, and for dimensionless rotational speeds of the cylinder, $0 \leq \Omega \leq 10$. The performance*
14 *of two turbulence methods, Large Eddy Simulation (LES) and Unsteady Reynolds-Averaged*
15 *Navier-Stokes (URANS), has been evaluated in this research. The flow and thermal fields are*
16 *studied through flow vectors, isotherm contours and iso-surfaces temperature, as well as*
17 *through the average Nusselt number (Nu_{av}) and velocity components. The results demonstrate*
18 *clearly that the flow patterns and the thermal fields are influenced strongly by increasing either*
19 *the rotating cylinder speed or the Reynolds number. Furthermore, both LES and URANS*
20 *solutions can capture the essential feature of the primary eddies in the cavity. But this study*
21 *has shown convincing evidence that only the LES method can predict the structure details of*
22 *the secondary eddies that have profound effects on the heat transfer behaviour within the*
23 *enclosure.*

24 **Keywords:** *Rotating cylinder, Lid-driven cavity, Mixed convection, Turbulent flow, URANS,*
25 *LES.*

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31 **1. Introduction**

32 Over the last few decades, the numerical simulations of turbulent flows and heat transfer have
 33 become one of the essential attentions of engineering applications in the industrial and
 34 engineering fields. Indeed, for high value Reynolds number turbulent flows, the expanded scope
 35 of turbulent vortices has gained major interests. Large Eddy Simulation (LES) method is
 36 increasingly involved in predicting the detailed turbulent flow scales [1, 2], though the
 37 Reynolds Averaged Navier-Stokes (RANS) approach is still a useful tool in evaluating the time
 38 averaged features of the turbulent flows [3-6]. Even though the LES costs more computational

Nomenclature			
CFL	Courant–Friedrichs–Lewy number	Y	distance along the non-dimensional y-coordinate (y/H)
D	width of the cavity on z-axis (m)	Z	distance along the non-dimensional z-coordinate (z/D)
d	cylinder diameter (m)		
FVM	finite volume method		
Gr	Grashof number ($g\beta_m\Delta TW^3/\nu_m^2$)	<i>Greek symbols</i>	
h	convective heat transfer coefficient (W/m ² K)	α	thermal diffusivity of the fluid (m ² /s)
k	turbulent kinetic energy (m ² /s ²)	β	volumetric coefficient of thermal expansion (1/K)
L	width of the cavity on x-axis (m)	μ	dynamic viscosity of the fluid (Pa/s)
Nu	Nusselt number	ν	kinematic viscosity of the fluid (m ² /s)
Pr	Prandtl number (ν_m/α_m)	ν_{sgs}	sub-grid scale (SGS) viscosity
Ra	Rayleigh number (Gr Pr)	ρ	density of the fluid (kg/m ³)
Re	Reynolds number ($U_{0,m}W/\nu_m$)	ε	dissipation rate of turbulent kinetic energy (m ² /s ³)
Ri	Richardson number (Gr/Re ²)	δ_{ij}	Kronecker's delta
\bar{S}_{ij}	large-scale strain rate tensor for grid-filter	$\bar{\Delta}$	grid-filter width
T	temperature of the fluid (K)	τ_{ij}	subgrid-scale (SGS) stress tensor
t	time	ω	rotational speed (rad/s)
u	velocity component at x-direction (m/s)	Ω	dimensionless rotational speed
U	dimensionless velocity component at x-direction		
U ₀	lid velocity (m/s)		
v	velocity component at y-direction (m/s)	<i>Subscripts</i>	
V	dimensionless velocity component at y-direction	av	average value
W	dimensionless velocity component at z-direction	b	buoyancy
x	distance along the x-coordinate	C	value of cold temperature
X	distance along the non-dimensional x-coordinate (x/L)	H	value of hot temperature
		rms	root mean square
		sgs	sub-grid scale
		t	turbulent

39 resources than the RANS modelling, this method performs better in terms of data availability
40 and accuracy [7].

41 The effect of combined natural convection, which emerges as a sequence of buoyancy effects,
42 with forced convection, which occurs as a result of the fluid motion due to shear forces that are
43 offered by external means such as the partial physical motion of the domain, is defined as mixed
44 convection. There have been quite a few studies over the last few years on heat convection
45 problems in the 2D cavities containing either a rotating or stationary cylinder with different
46 dimensionless diameters and boundary conditions. A 2D combined convection heat transfer of
47 heated top lid-driven wall cavity that has an internal central circular cylinder and heater was
48 simulated by Ray and Chatterjee [8]. It was demonstrated that the internal circular objects lead
49 to a considerable increment in the Nusselt number (Nu). A study of mixed and natural
50 convection of stationary and rotating centred cylinder in a 2D square cavity, with different
51 rotating speeds, was carried out by Liao and Lin [9]. It was concluded that by reducing the
52 Richardson number (Ri) the mean value of Nusselt number (Nu_{mean}) decreases. Heat transfer
53 was enhanced by using small aspect ratio between the inner cylinder and the outer cavity which
54 leads to generating a greater Nu. Hydro-magnetic mixed convection heat transfer in a 2D
55 moving wall cavity with central rotating conducting solid cylinder was demonstrated
56 numerically by Chatterjee, et al. [10]. It was summarised that an increase in rotation of the
57 conductive cylinder generates the enhancement of the heat transfer within the cavity.

58 Hussain and Hussein [11] numerically simulated laminar steady state mixed convection of air
59 within differentially heated cavity containing conductive rotating cylinder. It can be pointed out
60 that when the forced convection dominates, major vortices were founded around the cylinder.
61 No influences were noticed on both the flow and thermal fields when changing the cylinder
62 location at equal domination between the natural and forced convection. A natural convection
63 of a 2D square cavity with cold and hot cylinders was numerically investigated by Park, et al.
64 [12]. Different locations of cold and hot cylinders were the main concern. The outcome showed
65 that when the surfaces of the cylinders and the cavity were close to each other the Nusselt
66 number increases. An unsteady natural convection of two heated horizontal rotating cylinders
67 that erected within a 2D closed square cavity was simulated by Karimi, et al. [13]. It was
68 observed that at a low Rayleigh number (Ra) (less than 10^4) the distance between the cylinders
69 has a clear effect on the averaged-area of the Nusselt number. When the Rayleigh number is
70 higher than 10^4 and no more than 10^7 , the influence of spacing between the circular cylinders
71 could be ignored. A study of 2D natural convection in a closed square cavity with two horizontal

72 inner cylinders was numerically carried out by Yoon, et al. [14]. The upper cylinder was cooled,
73 while the lower one was heated. The lower and upper half of the cavity was the place of the
74 equidiameter cylinders. It was concluded that an increase in the radius of the cylinders at all
75 values of the Rayleigh number drives the increment of the heat transfer rate and dominates the
76 cold upper circular cylinder on a wider area.

77 An inner sinusoidally heated circular cylinder placed in a cavity was involved in a study of a
78 2D numerical unsteady natural convection heat transfer by Roslan, et al. [15]. It can be pointed
79 out that the flow field has two inner vortices and a heated cylinder provided a warm-chamber,
80 which impacts on the heat transfer. Although the heat transfer was not changed by changing
81 cylinder radius at the lowest value of the parameters, temporal increasing in the heat transfer
82 was found by increasing the cylinder radius to the maximum value of the dimensionless
83 parameters. In addition, it was observed that oscillating heat source of the cylinder caused
84 augment in the heat transfer rate. A natural convection of circular cylinder within a 2D rhombus
85 enclosure filled by water was numerically observed by Choi, et al. [16]. It was noticed that the
86 thermal features of the heat transfer between the cavity and its cylinder stick in accordance with
87 the value of the Rayleigh number and the cylinder location. Increasing Rayleigh number would
88 therefore lead to an increment in the Nusselt number for both the enclosure and its cylinder. In
89 addition, when the cylinder is located on the bottom wall of the rhombus cavity, the Nusselt
90 numbers for both the enclosure and its cylinder reach the maximum values. The lowest value
91 of the Nusselt numbers occurred when the cylinder was nearby the inner top of the cavity. The
92 investigations of mixed and natural convection of stationary and rotating with different rotating
93 speeds centred cylinder in a 2D square cavity study were carried out by Liao and Lin [9]. It was
94 figured out that a reduction in the Nusselt number happens when decreasing the Richardson
95 number. Heat transfer was enhanced by using the small aspect ratio that generates a greater
96 Nusselt number. The research of a heated hollow cylinder within the middle of the moving wall
97 enclosure was completed by Billah, et al. [17] at different range parameters, including the size
98 diameter of the cylinder, the Richardson number and the thermal conductivity of the fluid. The
99 sequences of installation cylinder on the mixed convection heat transfer coefficient were mainly
100 targeted. It has been noticed that a significant influence of the cylinder on the heat transfer ratio
101 as well as on the cylinder diameter size occurred. Khanafer and Aithal [18] evaluated a laminar
102 combined convection heat transfer and flow patterns of moving wall cavity that has a central
103 cylinder. It was concluded that the heat transfer fields can be controlled by the cylinder body
104 within the cavity. The obstacle size and location can affect the heat transfer and flow

105 characteristics. Laminar mixed convection of a heated square blockage within moving wall
106 enclosure was studied numerically by Islam, et al. [19] in order to understand the effects of the
107 central and eccentric locations of the square body at different sizes as well as the constant
108 Reynolds number on the heat transfer and flow patterns. It was observed that at the domination
109 of the forced convection there were no clear differences in the heat transfer when changing
110 either the location or the size of the installed body. An obvious influence was noticed on the
111 Nusselt number when the natural convection was controlling the domain.

112 A combined convection heat transfer of nanofluid in a 2D moving wall square cavity that
113 contains a rotating cylinder was studied numerically by Selimefendigil and Öztop [20]. It was
114 demonstrated that by increasing Ri , an increment of the heat transfer would occur. However,
115 by increasing the value of the Hartmann number the heat transfer reduces. The rotation of the
116 cylinder has a remarkable influence on the heat transfer enhancement. A 2D mixed convective
117 transport was investigated numerically by Chatterjee, et al. [21] in a moving top wall cavity
118 that includes a thermal adiabatic central rotating circular cylinder and this enclosure was filled
119 by Cu-water nanofluid. It was observed that the forced convection was dominated by fluid and
120 the heat transfer at the low value of the Ri number. By contrast, the natural convection has the
121 main effect on the heat transfer and fluid at a high Ri number. The drag coefficient of the
122 moving lid-driven wall incremented by increasing the speed of the rotating cylinder and by
123 increasing the Ri number. Thus, increasing Ri enhances the Nusselt number on the heated wall.
124 The study of both mixed convection heat transfer and flow patterns of rotating cylinder within
125 an obstructed cavity, filled by nanofluid, is completed by Roslan, et al. [22]. It was concluded
126 that the heat transfer can be increased due to the increment in nanoparticles concentration.
127 Besides, the positive effect of the rotating speed on the heat distribution and the effect of the
128 radius size of the cylinder on the fluid behaviours were reported. Combined convection of heat
129 transfer and fluid structure of a 2D differentially heated square cavity containing a central
130 rotating cylinder is simulated numerically by Costa and Raimundo [23] who investigated the
131 effects of the rotating cylinder size and rotation speed. It was demonstrated that discernible
132 influences on the heat transfer and fluid characteristics have been noticed by changing either
133 the cylinder size or its rotation speed. Overall, it can be seen from the previous work that only
134 limited investigations have been completed on the heat convection in cavities that are filled by
135 nanofluids [20-30]. These studies take into account the influences of the nanoparticles type,
136 size and concentration on the heat transfer in various cases besides the effects of the inner
137 cylinders.

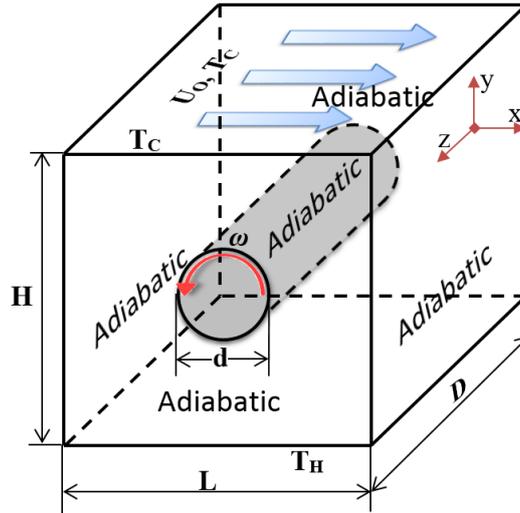
138 Recently, some interesting studies have been completed on 2D mixed convections of moving
139 walls cavities filled by nanofluids. The effects of inclined magnetic field and discrete heating
140 of double lid-driven enclosure of a 2D MHD mixed convection of nanofluid was studied by
141 Hussain, et al. [31]. Investigating the influences of inclination angles on the combined
142 convection of laminar nanofluid flow within a 2D lid-driven cavity has been achieved
143 numerically at several dimensionless parameters [32]. Inserting an isothermal square object
144 within a moving wall enclosure filled by nanofluids to study mixed convection heat transfer
145 enhancement has been numerically accomplished by Mehmood, et al. [33].

146 By considering the literature review and to the authors' best knowledge, it can be concluded
147 that only the 2D mixed convection heat transfer in a plane moving wall square cavity with
148 rotating cylinder was studied using either classic fluids or nanofluids. However, no researcher
149 has given attention to the LES modelling of the 3D mixed convection within a cubic enclosure
150 with a rotational cylinder and comparing it to the URANS modelling. Therefore, filling this gap
151 will form the main investigation objectives of this paper.

152 **2. Numerical model**

153 *2.1 Physical model*

154 The schematic diagram and main geometry parameters of the cubic moving wall cavity with
155 rotating cylinder are shown in [Fig. 1](#). The top wall of the cubic enclosure is treated as a cold
156 moving wall, while the bottom wall is maintained at hot constant temperature. The rest walls
157 of the geometry are assumed thermally adiabatic and stationary except the central cylinder
158 which is assumed as a rotating part (anti-clockwise).



159

160 **Fig. 1.** Schematic geometry of the cubic lid-driven cavity with rotating cylinder

161 *2.2 Governing equations*

162 The governing equations of the continuity, momentum and energy are written below in this
 163 work for three-dimensional turbulence flow and heat transfer in an incompressible Newtonian
 164 fluid [34-36].

Continuity equation:

$$\frac{\partial \rho}{\partial t} + \frac{\partial u_i}{\partial x_i} = 0 \quad (1)$$

Momentum equation:

$$\frac{\partial u_i}{\partial t} + \frac{\partial (u_j u_i)}{\partial x_j} = -\frac{\partial P}{\partial x_i} + \frac{1}{Re} \left(\frac{\partial^2 u_i}{\partial x_i \partial x_i} \right) + \frac{Gr}{Re^2} \theta \quad (2)$$

Energy equation:

$$\frac{\partial (\theta)}{\partial t} + \frac{\partial (u_j \theta)}{\partial x_j} = \frac{1}{RePr} \left(\frac{\partial^2 \theta}{\partial x_i \partial x_i} \right) \quad (3)$$

The turbulent kinetic energy (k) and the dissipation rate (ε) are respectively shown below in equations (4) and (5) [37].

Standard k-ε turbulence model:

$$\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] + P_k + P_b - \rho \varepsilon + S_k \quad (4)$$

$$\frac{\partial}{\partial t}(\rho \varepsilon) + \frac{\partial}{\partial x_i}(\rho \varepsilon u_i) = \frac{\partial}{\partial x_j} \left[\left(\mu + \frac{\mu_t}{\sigma_\varepsilon} \right) \frac{\partial \varepsilon}{\partial x_j} \right] + C_{1\varepsilon} \frac{\varepsilon}{k} (P_k + C_{3\varepsilon} P_b) - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k} + S_\varepsilon \quad (5)$$

where S_k and S_ε refer to the user-defined source terms, and $C_{1\varepsilon}$, $C_{2\varepsilon}$ and $C_{3\varepsilon}$ are model constants. Some other terms in the equations are defined below.

Turbulent viscosity:
$$\mu_t = \rho C_\mu \frac{k^2}{\varepsilon} \quad (6)$$

Production of k:
$$P_k = -\rho \overline{u'_i u'_j} \frac{\partial u_j}{\partial x_i} \quad (7)$$

Effect of buoyancy:
$$P_b = \beta g_i \frac{\mu_t}{Pr_t} \frac{\partial T}{\partial x_i} \quad (8)$$

For the LES work, the sub-grid scale (SGS) model of WALE (Wall-Adapting Local Eddy-viscosity) is employed, as given by Nicoud and Ducros [38] and Ben-Cheikh, et al. [7]:

$$\mu_t = \rho L_s^2 \frac{(S_{ij}^d S_{ij}^d)^{\frac{3}{2}}}{(\bar{S}_{ij} \bar{S}_{ij})^{\frac{5}{2}} + (S_{ij}^d S_{ij}^d)^{\frac{5}{2}}} \quad (9)$$

where L_s and S_{ij}^d are defined below:

$$L_s = \min \left(kd, C_W V^{\frac{1}{3}} \right) \quad (10)$$

where $C_W = 0.325$

$$S_{ij}^d = \frac{1}{2} (\bar{g}_{ij}^2 + \bar{g}_{ji}^2) - \frac{1}{3} \delta_{ij} \bar{g}_{kk}^2 \quad (11)$$

$$\text{where } \bar{g}_{ij} = \frac{\partial \bar{u}_i}{\partial x_j} \quad (12)$$

$$\bar{S}_{ij} = \frac{1}{2} \left(\frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) \quad (13)$$

166 2.3 Boundary conditions

167 The boundary conditions for the current study are defined as:

168 Top wall:

$$169 \quad \partial\theta/\partial Y = 0, U = 1, V = 0, W = 0$$

170 Bottom wall:

$$171 \quad \partial\theta/\partial Y = -1, U = 0, V = 0, W = 0$$

172 Other walls:

$$173 \quad \theta = 0, U = 0, V = 0, W = 0$$

174 Cylinder:

$$175 \quad \omega = \frac{\Omega \times 2U_0}{d}, d = 0.2L, \theta = 0$$

176 2.4 Numerical procedure

177 The numerical simulations of fluid flow and heat transfer were conducted by utilizing the
178 Computational Fluid Dynamic (CFD) techniques. The finite volume method (FVM) and
179 SIMPLEC algorithm were used to discretize the governing equations and to deal with the
180 pressure-velocity coupling equations. The commercial code ANSYS©FLUENT (version
181 R16.2) [39] was adapted to complete the simulations. Both steady and unsteady Reynolds-
182 averaged Navier–Stokes equations were solved besides the large eddy simulation method. The
183 QUICK and implicit second order scheme were used to respectively deal with the convection
184 and the time evaluation terms. The CFD results were collected when the convergence criteria
185 of 10^{-5} were satisfied at each time step.

186 3. Results and discussion

187 This phase aims to understand and explore the combined impacts of the moving wall and
188 rotating cylinder on the heat convection and flow patterns under turbulent flow conditions. The
189 completed simulations include four Reynolds numbers, $Re = 5000, 10000, 15000$ and 30000 ,
190 and four cylinder rotation speed values, $\Omega = 0, 1, 5$ and 10 .

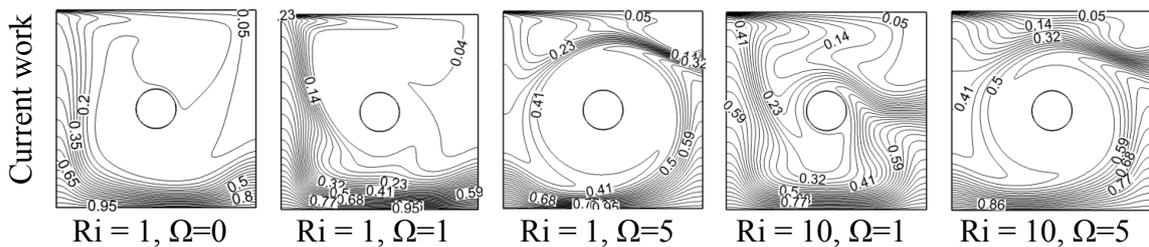
191 *3.1 Mesh independence test*

192 It is known that the grid independence test plays a considerable role in a CFD simulation
 193 regarding the results prediction time and accuracy. The mesh features such as density and
 194 quality were carefully considered in this study to avoid the numerical errors and to reach better
 195 computational efficiency. Structured and non-uniform cells were created in this work by Fluent
 196 ICEM 16.2 [39]. In addition, the meshes nearby the walls are refined, particularly in the area
 197 close to the circular cylinder. The generated grids of the whole domain were fine enough to
 198 capture the details of the fluid structures and thermal distribution within the cavity. Several grid
 199 numbers (125868, 292440, 496800, 929160 and 1260762) were tested in order to figure out the
 200 suitable mesh number. The final chosen number of grid points in the current study was 929160,
 201 which was proved satisfactory by different indicators that are important in order to obtain high
 202 quality results: the non-dimensional time step is 0.004, the dimensionless wall distance $y^+ \approx 1$
 203 and the Courant-Friedrichs-Lewy number $CFL = 0.3$. Moreover, the minimum orthogonal
 204 quality is 0.7267 and the aspect ratio changes from less than 8 in the key interesting areas to
 205 27.326 far away from the domain walls and the circular cylinder.

206 *3.2 Code validations*

207 The validation of the 2D rotating solid cylinder within a moving wall cavity is achieved in this
 208 section. The comparison is made by using the following dimensionless parameters: $Gr = 10^4$,
 209 $Pr = 6.95$, $1 \leq Ri \leq 10$ and $1 \leq \Omega \leq 10$. The RANS simulation findings are compared with the
 210 experimental measurements by Chatterjee, et al. [21] in terms of isotherms, streamlines
 211 contours and dimensionless velocity profiles along the vertical line at $x = 0.25$. An excellent
 212 agreement is accomplished as shown in Fig. 2, Fig. 3 and Fig. 4. Moreover, as shown in Fig. 5,
 213 the LES prediction from the current work of a 3D lid-driven enclosure is compared to the
 214 experimental outcomes of Prasad and Koseff [40] and the RANS results of Peng, et al. [41] in
 215 term of mean velocity of turbulent flow. Distinctly, the current simulation results are in good
 216 agreement with those from the previous publications. Overall, the validations prove that the
 217 present simulation methods are highly reliable and accurate.

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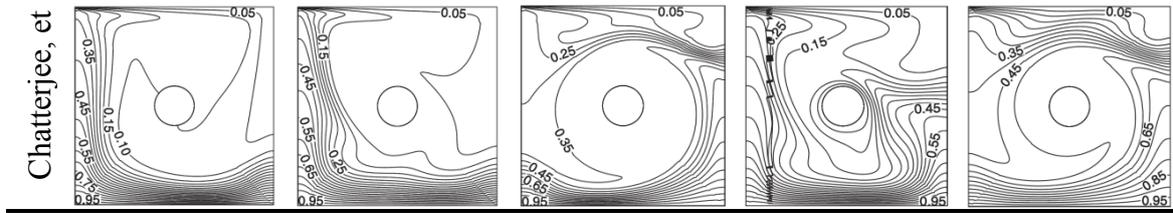


Fig. 2. Comparison of the present work of the isotherms with Chatterjee, et al. [21].

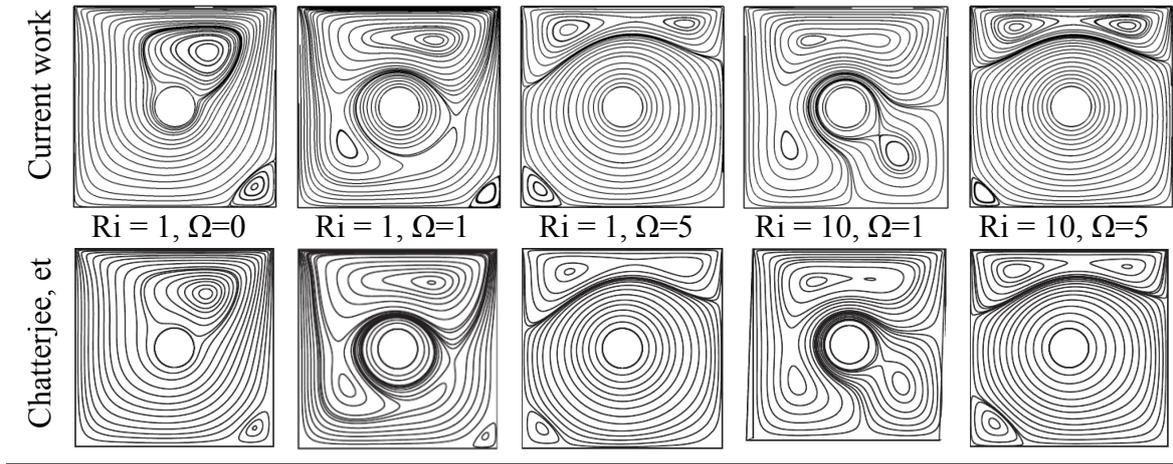


Fig. 3. Comparison of the present work of the streamlines with Chatterjee, et al. [21].

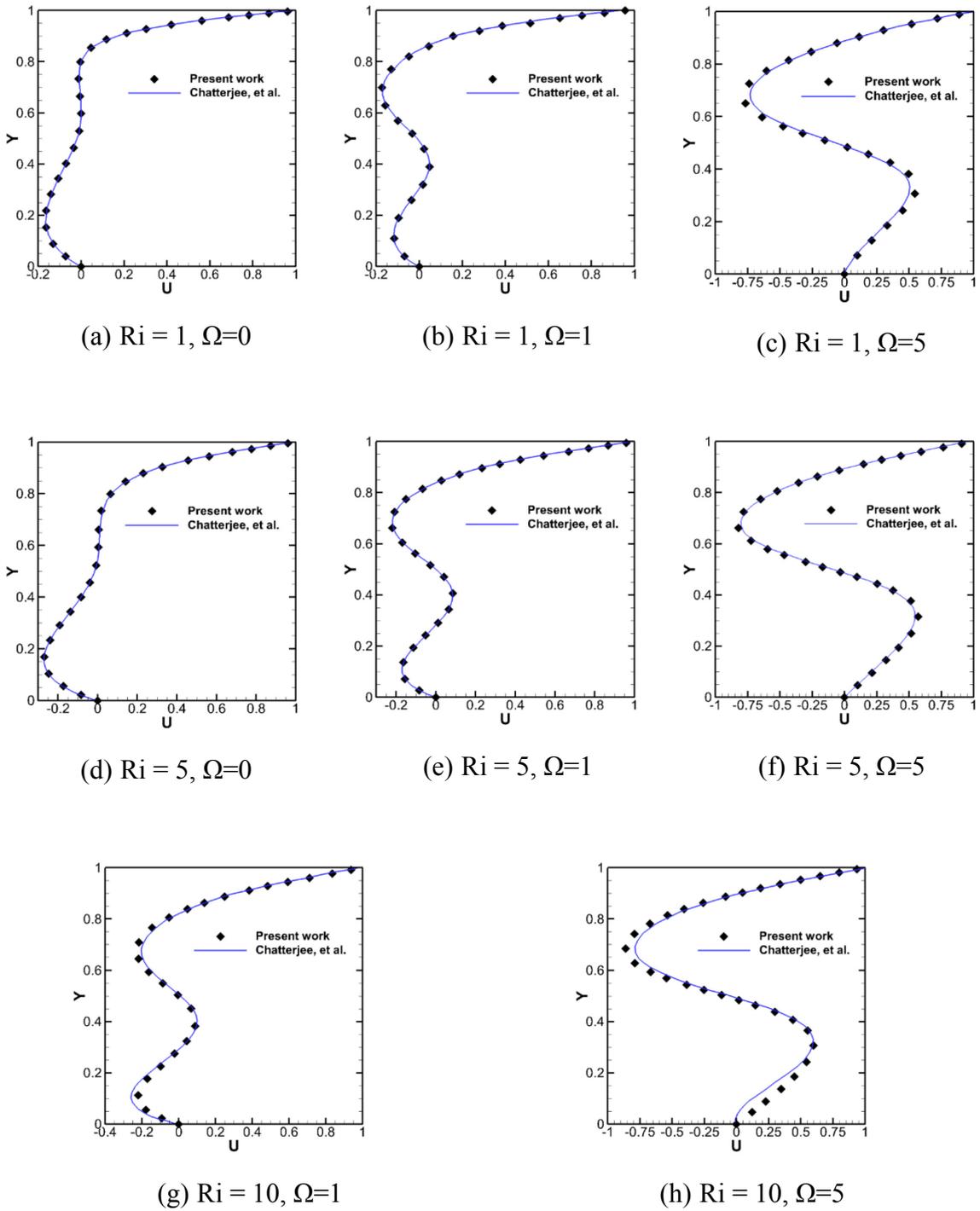
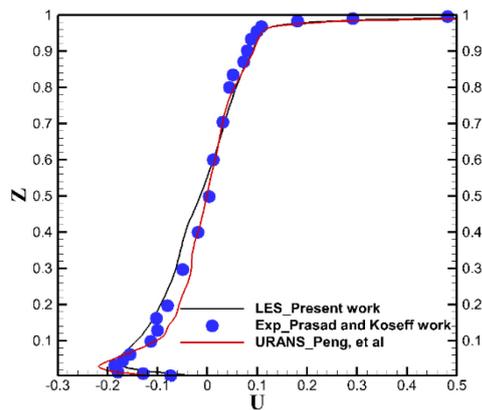
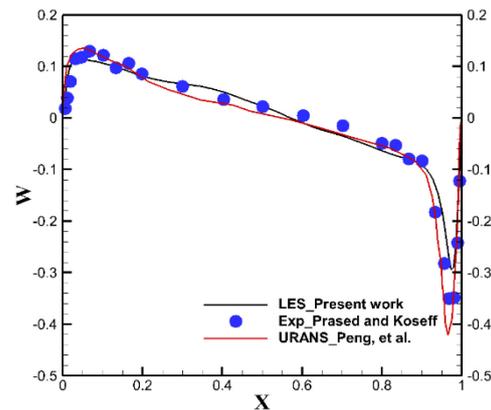


Fig. 4. Comparison of the present work of the dimensionless velocity profiles along the vertical line at $x = 0.25$ with Chatterjee, et al. [21].



(a) Left velocity



(b) Right velocity

Fig. 5. Mean velocity profiles comparison of the current LES work with Prasad and Koseff [40] and Peng, et al. [41] at $Re = 10000$.

222

223 3.3 RANS model

224 The Reynolds-averaged Navier–Stokes equations are known as the time-averaged equations of
 225 movement for the fluid flow. This section is completed by using the RANS method to study the
 226 flow and thermal fields and velocity distribution in a 2D lid-driven enclosure that contains a
 227 rotating circular cylinder.

228 3.3.1 Flow and thermal fields

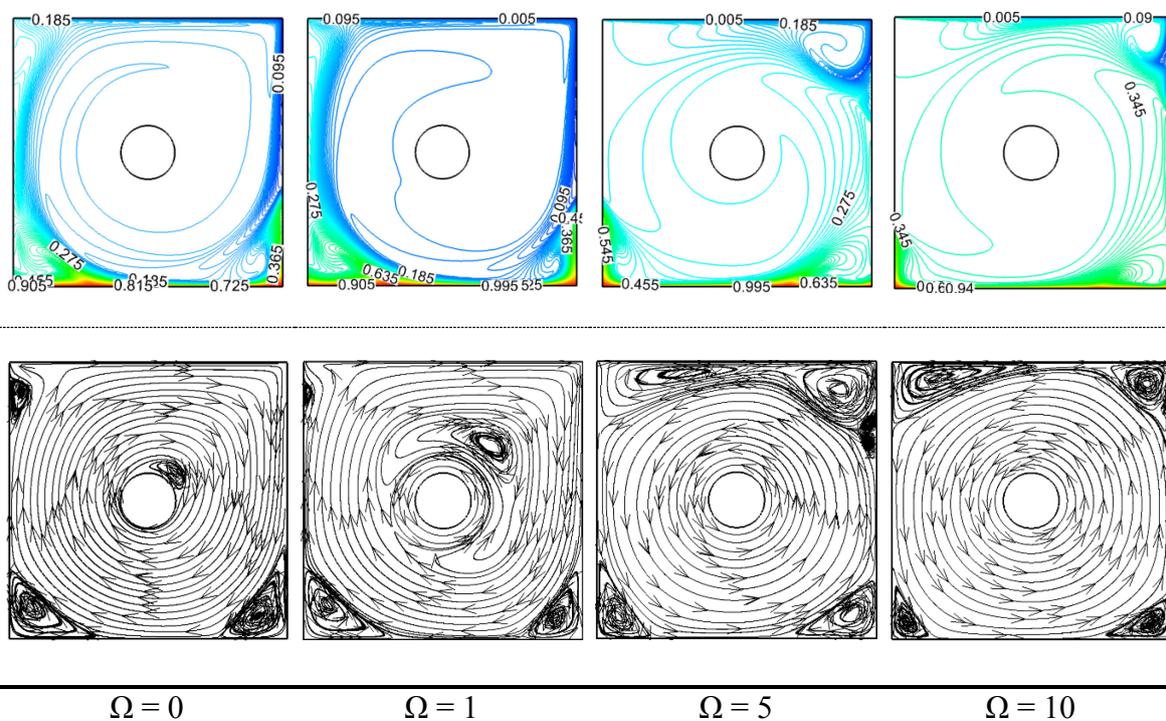
229 Isotherms and streamlines contours are plotted in Fig. 6 at various controlling parameters,
 230 Reynolds numbers, $Re = 5000, 10000, 15000$ and 30000 , and rotational speeds, $\Omega = 0, 1, 5$ and
 231 10 . These contours arise by the coupled impacts of forced shear flow (rotating cylinder and
 232 moving top wall forces) besides the buoyancy flow due to the heat differences between the top
 233 and bottom walls. It can be observed that the influences of both forced actions are dominated
 234 on most of the heat distribution and flow patterns within the enclosure, aside from the minor
 235 effect of the driven buoyancy. Substantially, the shear layers are generated nearby the moving
 236 objects and their magnitudes totally depend on the values of the speed of the rotating cylinder
 237 and the moving top wall.

238 At all values of the Reynolds number and when the inner cylinder is stationary ($\Omega = 0$), the flow
 239 field patterns are the consequence of the moving-lid movement and the temperature differences.
 240 A clockwise rotating primary eddy, which is formed as a result of the movement of the lid, is
 241 encased in most of the cavity besides four small secondary eddies which are placed at the

242 bottom wall corners (anti-clockwise), the top of the left wall (anti-clockwise) and the right top
 243 of the cylinder (clockwise). It can be observed that increasing Reynolds number leads to
 244 decreasing the secondary eddies sizes.

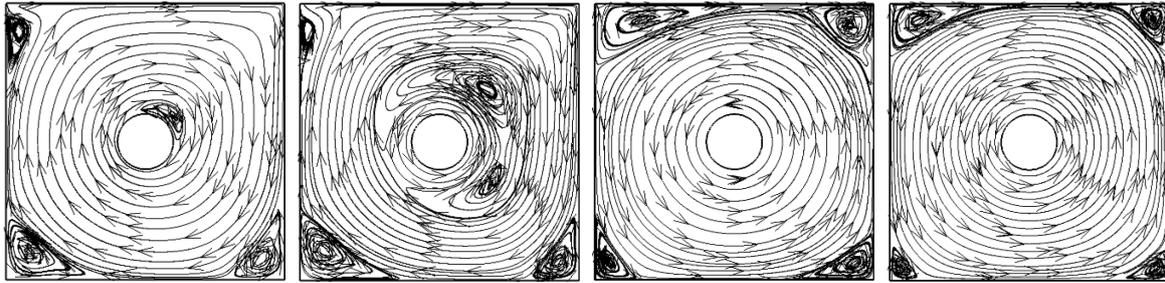
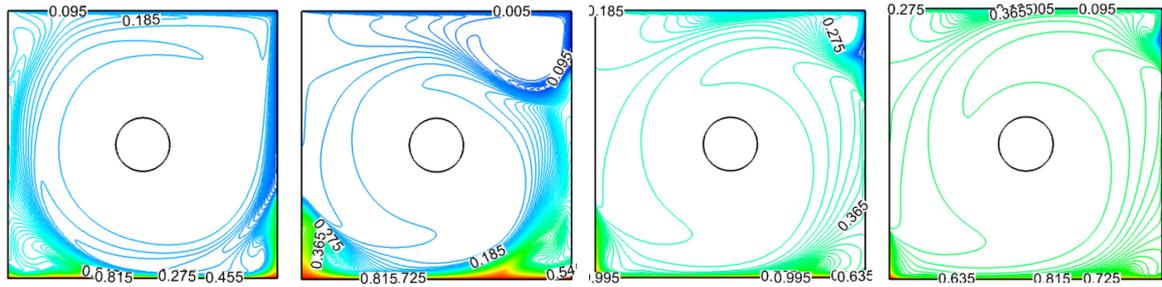
245 Whilst the inner cylinder is rotating at low velocity value, $\Omega = 1$, the flow field's evolution
 246 results from the combined action of the lid-driven movement, the rotating cylinder motion and
 247 the buoyancy driven effect. Although some shear layers appear thereabout the inner cylinder at
 248 all Reynolds number values, the domination of the main eddy, which is formed by the linear
 249 movement of the top wall, covers most of the enclosure regions. However, the influence by the
 250 movement of the rotating cylinder is increased by using high values of rotational speed, $\Omega = 5$
 251 and $\Omega = 10$. Consequently, it can be seen that the effect of the linear movement of the top wall
 252 appears as two clockwise vortices and adjacent to the top surface of the cavity. In addition, the
 253 two anti-clockwise eddies nearby the bottom walls became clockwise when the rotating speed
 254 controls most of the enclosure zones.

255 In general, an increment in linear speed of the lid-driven or in rotation speed of the inner
 256 cylinder provides better temperature distribution in the domain, and more particularly when
 257 both speeds are high ($Re = 30000$ and $\Omega = 10$).



(a) $Re = 5000$

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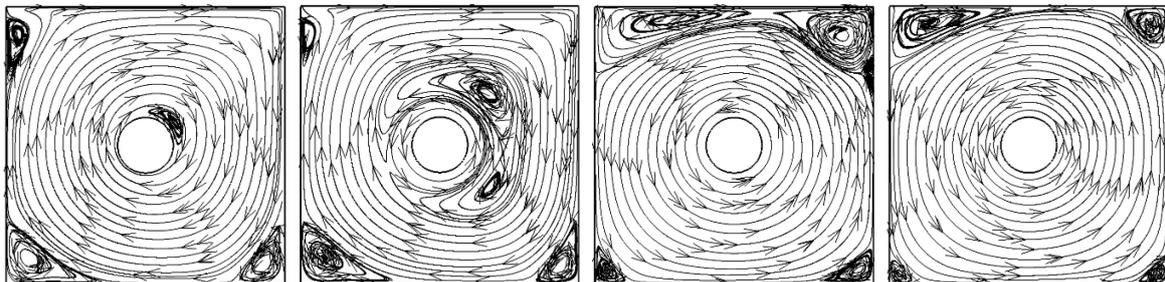
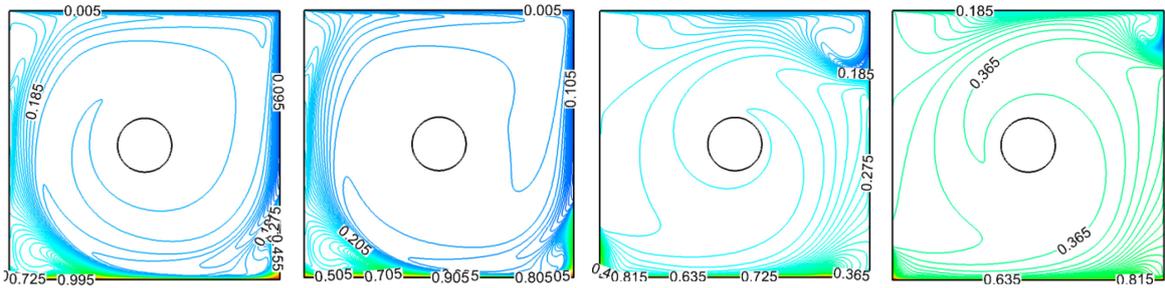
$\Omega = 0$

$\Omega = 1$

$\Omega = 5$

$\Omega = 10$

(b) $Re = 10000$



$\Omega = 0$

$\Omega = 1$

$\Omega = 5$

$\Omega = 10$

(c) $Re = 15000$

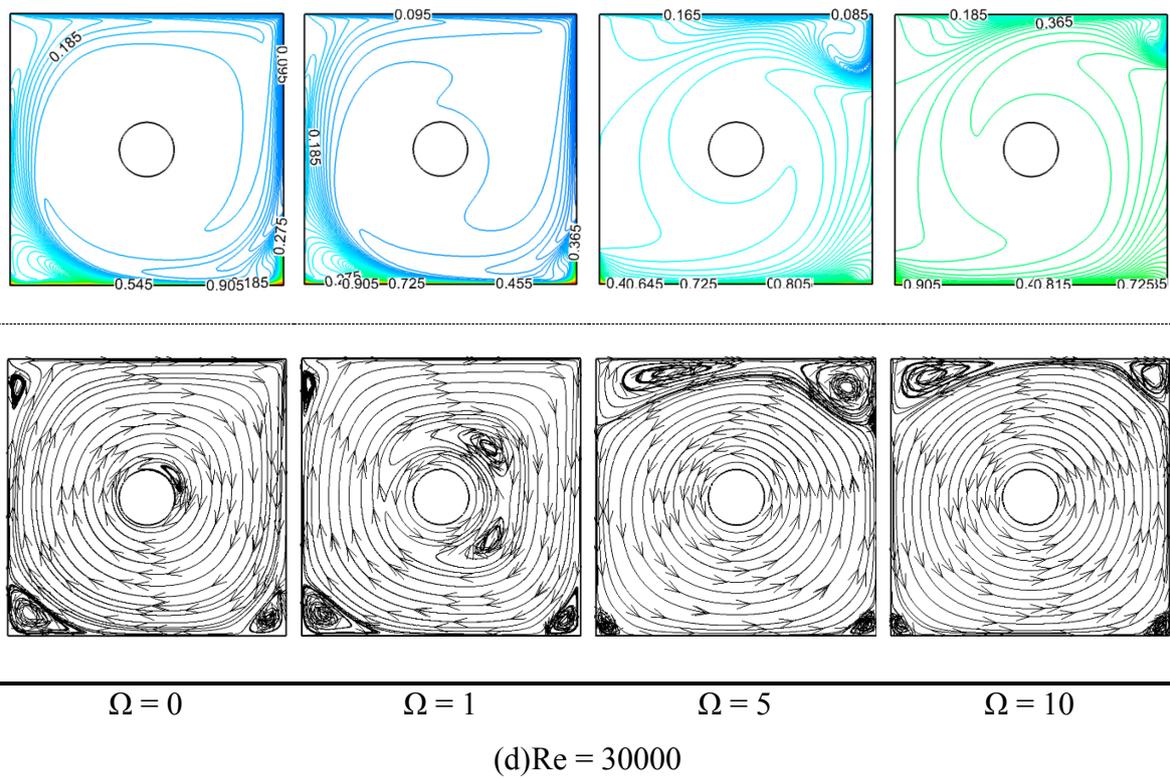


Fig. 6. Isotherms and streamlines contours for different Reynolds numbers and rotating speeds.

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261 3.3.2 Velocity distribution

262 The curves of the dimensionless horizontal velocity distribution along the vertical line, that is
 263 located at $(0.25, 0, 0)$ and $(0.25, 1, 0)$, for various values of the Reynolds number, $Re = 5000$ -
 264 30000 , and rotational velocity, $\Omega = 0 - 10$, are presented in Fig. 7. Slight differences can be
 265 figured out when the rotational speed is equal to zero or one, unlike when the rotating cylinder
 266 dominates the flow patterns at high Ω values. Moreover, it can be concluded that Reynolds
 267 number can change the values of the velocity distribution, while the rotating cylinder is holding
 268 the direction of the flow in the cavity.

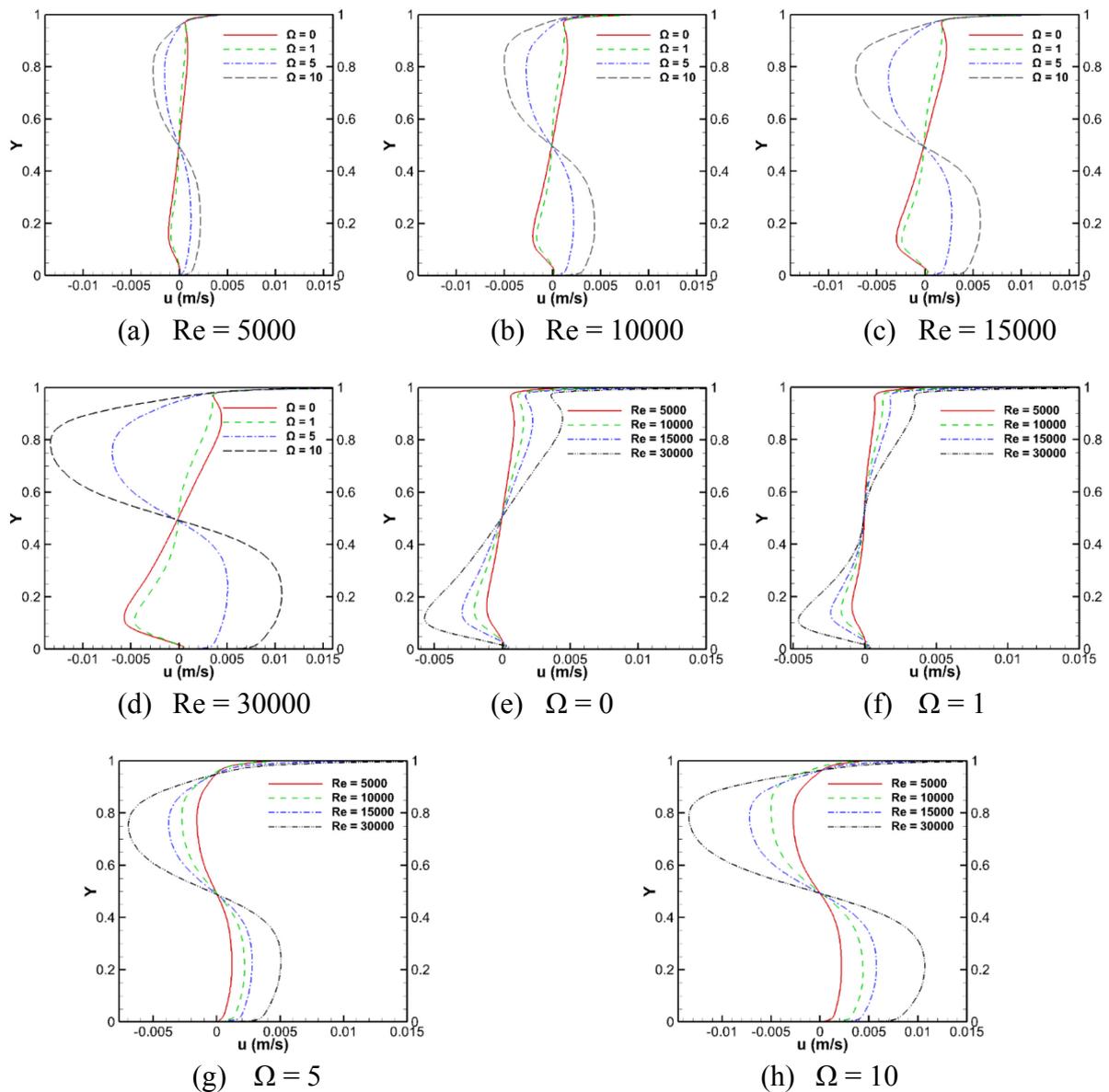


Fig. 7. Velocity distribution along the vertical line for different Reynolds numbers and rotational speeds.

269

270 3.4 URANS model

271 The Unsteady Reynolds-averaged Navier–Stokes equations depend on the time-averaged
272 equations of movement for the fluid flow. However, their mean flow quantities keep changing
273 with time step. This section is completed by using the URANS method to investigate the heat
274 transfer characteristics and Nusselt number in a 3D lid-driven enclosure containing a rotating
275 circular cylinder.

276 3.4.1 Heat transfer characteristics

277 Fig. 8 illustrates the influences of varying rotational speeds of the cylinder, $\Omega = 0, 1, 5$ and
278 Reynolds numbers, $Re = 5000, 10000$ and 15000 , on three-dimensional profiles of the isotherms
279 and its iso-surface temperatures for the nine cases studies of the cavity in order to understand
280 the flow patterns and the related heat distribution. It can be observed that when the
281 dimensionless rotational velocity is stationary, $\Omega = 0$, the top moving wall is controlling all the
282 fluid behaviours and the heat transfer distribution besides the limited buoyancy effect due to
283 the different temperatures of the top and bottom walls. It can be noticed that the flow direction
284 is clockwise. However, when the cylinder is moving in rotational direction at rotating speed
285 equal to one, it can be argued that the rotating force controls the region around the cylinder
286 whereas most of the area of the enclosure is driven by the moving top wall. By comparison to
287 the rotating speed equal to five, this measure shows that most of the cavity's area is covered by
288 the affected flow due to the rotating cylinder's force. Nonetheless, in both cases ($\Omega = 1$ and 5)
289 it can be seen that the homogeneity of the temperature division inside the domain is higher than
290 that in the stationary cylinder case.

291

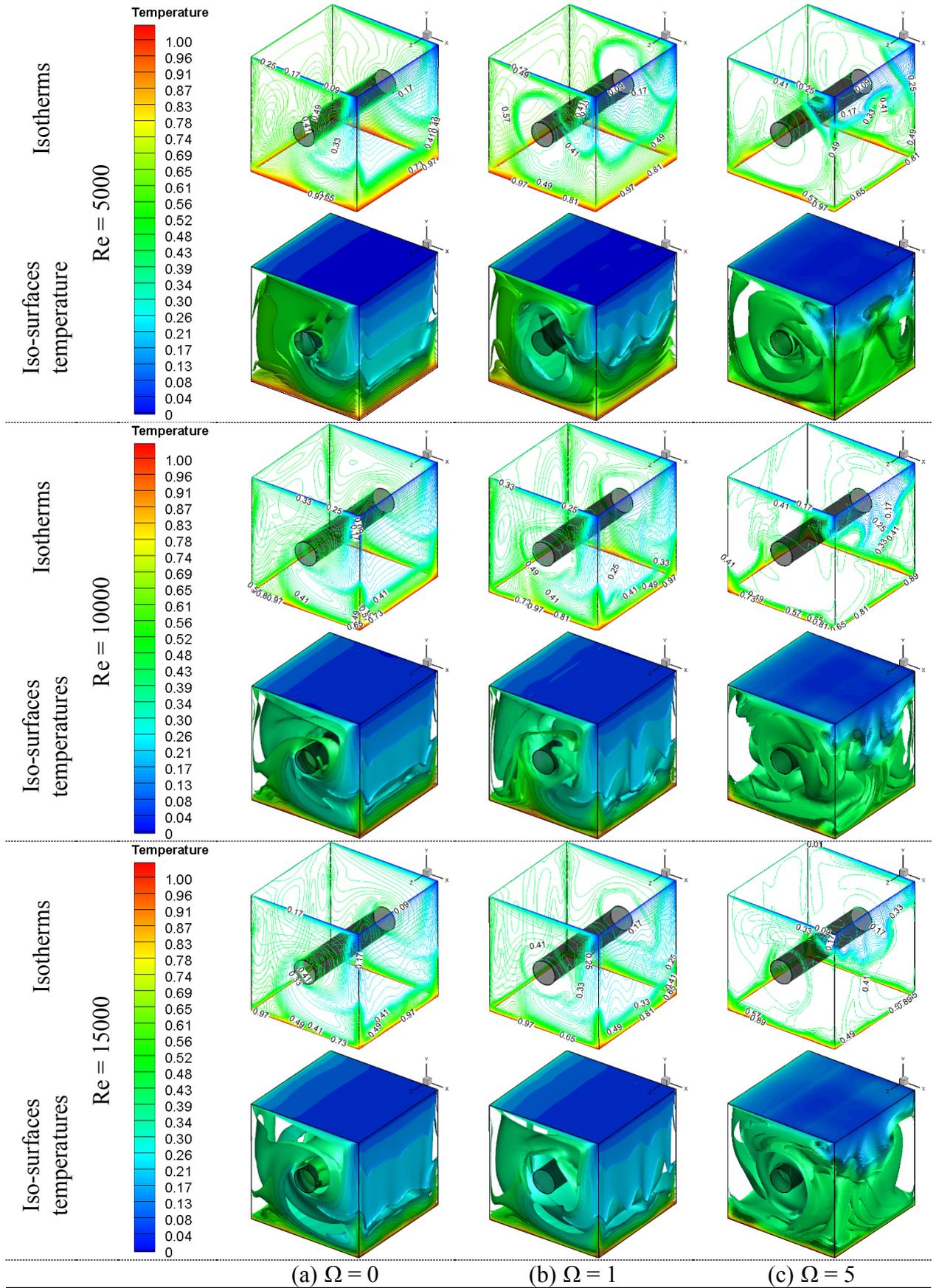


Fig. 8. Three-dimensional isotherms and iso-surfaces temperatures at different Reynolds numbers and rotational speeds.

292 3.4.2 Nusselt number

293 Fig. 9 shows the average Nusselt number for the chosen values of rotational speed, $\Omega = 0, 1$
 294 and 10, and Reynolds number, $Re = 5000, 10000$ and 15000 , at the midline of the bottom wall.
 295 The Standard $k-\epsilon$ viscous model with time dependence is exercised in this investigation.
 296 Essentially, the figure illustrates that increasing either Re or Ω values leads to a remarkable
 297 enhancement in the average Nusselt number which is mainly the consequences of the increased
 298 flow velocity. Since higher motion of the fluid occurs at higher Reynolds number and rotation
 299 speed, it can be concluded that the highest Nusselt number occurs when Reynolds number
 300 $=15000$ and the rotational speed $= 10$.

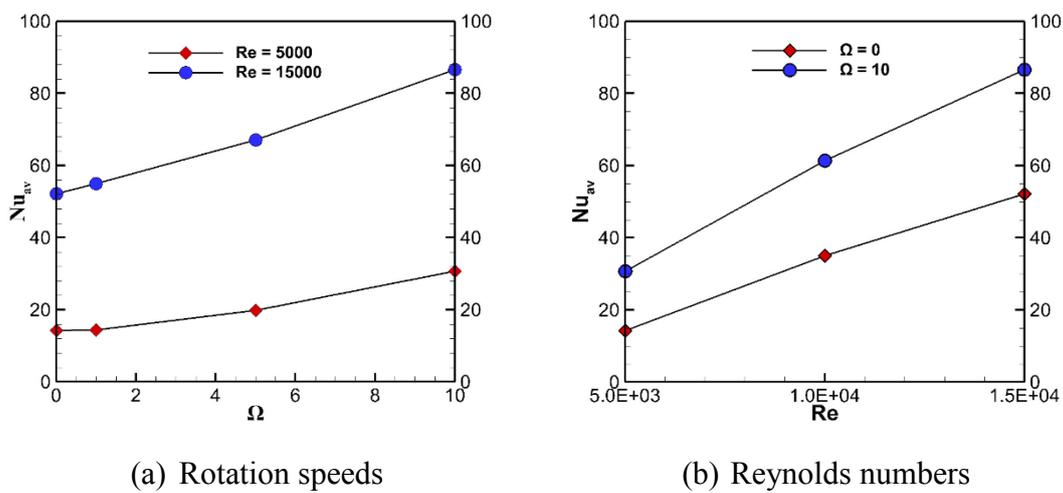


Fig. 9. Average Nusselt number distributions at the bottom wall for different Reynolds numbers and rotational cylinder speeds.

301
302

303 The local Nusselt number distributions along the midline of the heated top wall (0, 1, 0.5 and
 304 1, 1, 0.5) are shown in Fig. 10 for various values of the rotational speed and Reynolds number.
 305 Essentially, it demonstrates that Reynolds number has a meaningful effect on the top wall local
 306 Nusselt number for all the cylinder rotational speeds. On the other hand, at rotational speed, 0
 307 $\leq \Omega \leq 5$, and at all Reynolds number values, $Re = 5000 - 15000$, it can be noticed that by
 308 changing the rotational speed no distinct change has been detected on the top moving wall local
 309 Nusselt number. This can be clarified as the consequences of the strong domination of the lid-
 310 driven motion on the heat transfer of the top wall. However, when the rotational speed is equal
 311 to 10, it can be observed the clear influences of the rotating cylinder on the top wall heat
 312 transfer. These influences increase gradually as increasing Reynolds number.

313

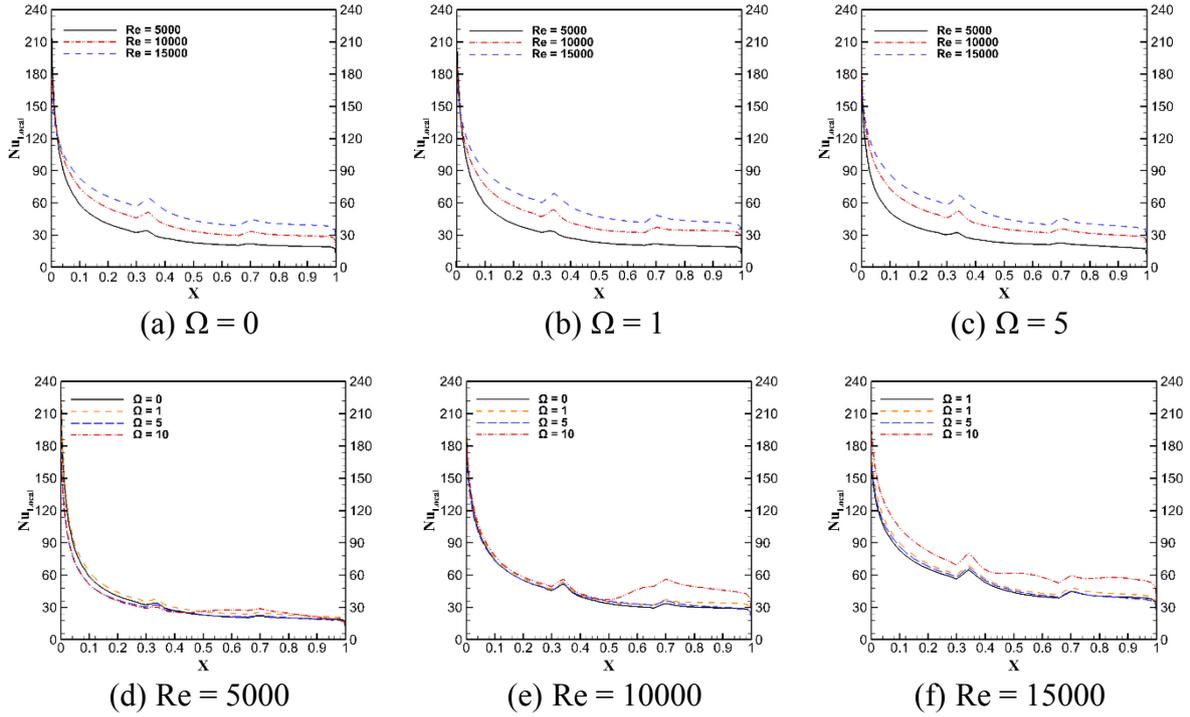
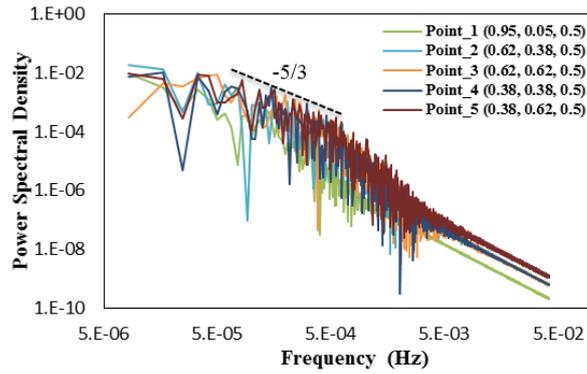


Fig. 10. Local Nusselt number of the top moving wall for different Reynolds numbers and rotational cylinder speeds.

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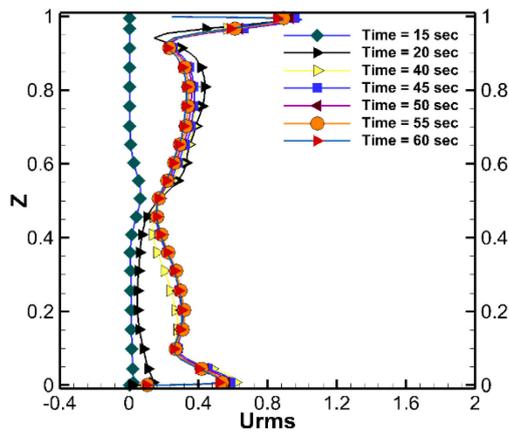
315 3.5 Comparison between URANS and LES

316 Hereinafter, inclusive comparison and discussion will be focused on the findings generated
 317 from simulating the unsteady turbulent flow of combined convection heat transfer in the lid-
 318 driven cavity containing rotating circular cylinder by involving the WALE sub-grid scale model
 319 of the LES method and the standard $k-\epsilon$ model of the URANS method. The simulations are
 320 completed for two Reynolds numbers, $Re = 5000$ and 10000 , and three rotational speeds, $\Omega =$
 321 $0, 1$ and 5 . The outcomes and comparisons are presented in terms of velocity vectors, isotherms,
 322 iso-surfaces temperatures and local Nusselt numbers. The spectral density profiles of the
 323 velocity magnitude at five selected points within the domain in order to confirm the LES
 324 simulations are correctly performed are shown in Fig. 11 for $Re = 10000$ and $\Omega = 1$. It can be
 325 noticed that the slope of $-5/3$ in the inertial subrange is observed, showing that the present
 326 simulations can be regarded as having the features of a fully turbulent flow. In addition, the
 327 results of the LES method are accepted only after reaching the fully developed flow state. Fig.
 328 12 illustrates the U_{rms} profile evolution along a line located in the cavity at $(0.25, 1, 0.5)$ and
 329 $(0.25, 0, 0.5)$ for different simulation times. It can be seen that after 45 seconds, the flow reaches
 330 the steady state. However, the statistical simulations results are collected after 50 seconds to
 331 ensure their high quality.



332

333 **Fig. 11.** Spectral analysis of velocity magnitude at selected locations for $Re = 10000$, $\Omega = 1$.



334

335 **Fig. 12.** Root mean square velocity profiles at different simulation times

336 *3.5.1 Three-dimensional isotherms and iso-surface temperatures*

337 The computational results from the LES and URANS methods are compared at chosen
 338 rotational speeds of the circular cylinder, $\Omega = 0, 1$ and 5 , and Reynolds numbers, $Re = 5000$.
 339 The three-dimensional isotherms and iso-surfaces temperatures are offered in **Fig. 13** to analyse
 340 the differences between the LES and URANS behaviours. Generally, for stationary cylinder it
 341 can be argued that the moving top wall is controlling the flow patterns and the heat transfer.
 342 However, for $\Omega = 1$, it can be noticed that the force that comes from the rotational cylinder
 343 starts influencing the central part of the enclosure. This influence is growing strongly when the
 344 rotational speed reaches five. Hence, increasing the rotational speed enhances significantly the
 345 heat transfer distribution.

346 In comparison of the turbulent prediction approaches, it can be pointed out from the shown
 347 figure that both methods have demonstrated a good ability of showing the primary vortices of
 348 the flow for all cases shown in **Fig. 13**. However, the secondary vortices appear clearly by using

349 the LES prediction and these vortices increase at either a higher Reynolds number or a higher
 350 rotational speed.

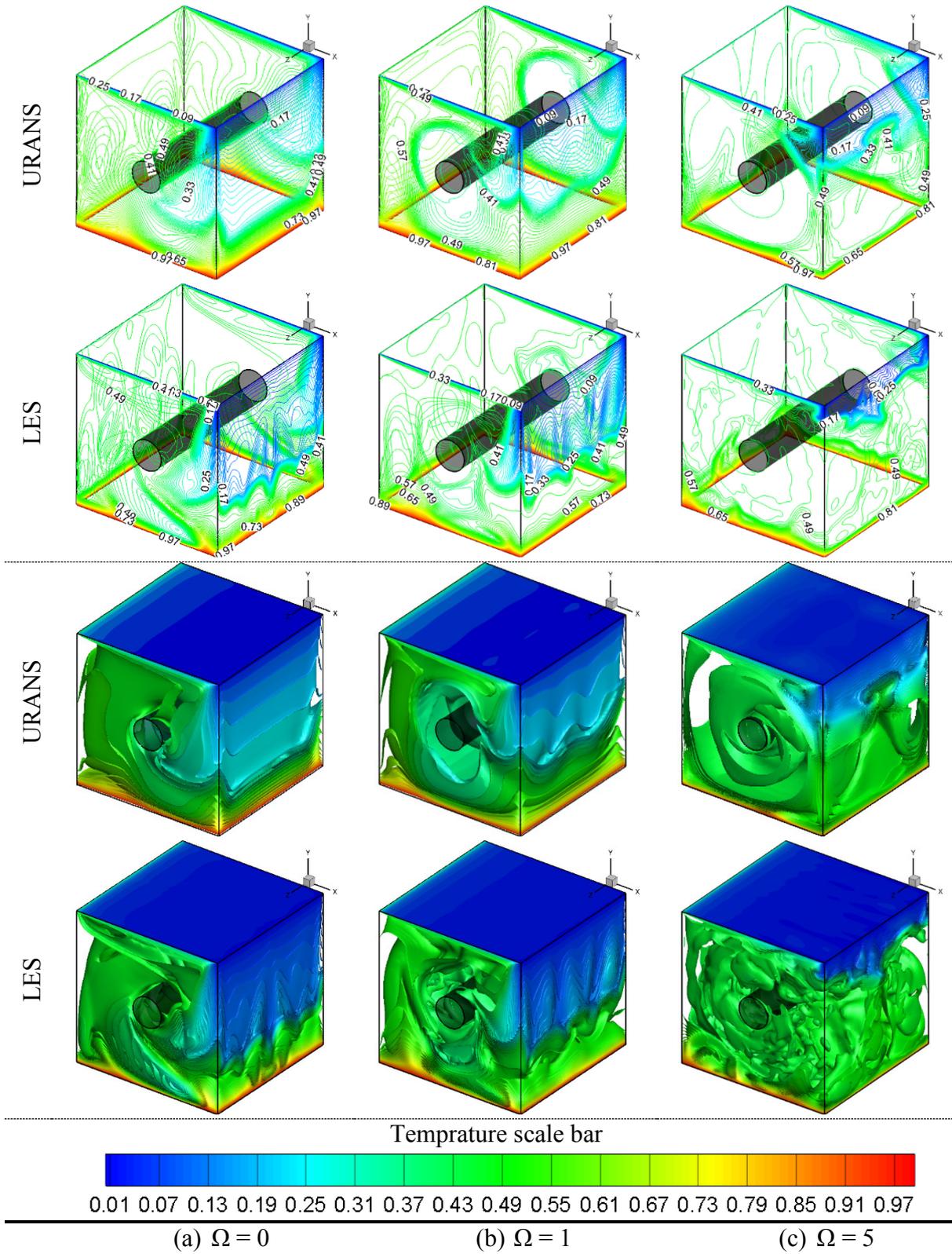


Fig. 13. Three-dimensional isotherms and iso- surfaces temperatures distribution comparison of URANS and LES at $Re = 5000$.

353 3.5.2 *Velocity vectors*

354 The flow vectors of both URANS and LES methods have been investigated for Reynolds
355 number, $Re=5000$, and rotating speed, $\Omega = 0, 1$ and 5 . Fig. 14a illustrates the flow behaviours
356 for the y-z plane located in the middle of the z-axis, and Fig. 14b states the x-y plane located in
357 the midway of the x-axis. Generally, for both approaches and when the circular cylinder is
358 stationary, it can be noticed that the controlling influence of forced convection is due to the
359 moving top wall, especially for the layers nearby the lid-driven wall. The flow nearby the lid-
360 driven wall is drawn due to the shear force and it impinges onto the motionless-walls. The
361 primary vortex (rotating clockwise) covering the domain centre is distinctly seen in Fig. 14b
362 and this vortex controls most of the flow patterns, as predicted by either URANS or LES
363 method. Further, the displayed vectors in Fig. 14 reveal the presence of the secondary vortices
364 thereabout the domain corners and the top right of the cylinder. However, it can be observed
365 distinctly that the secondary vortices become more visible from the LES prediction for both
366 selected planes, especially when increasing the rotational speed of the cylinder.

367 The superiority of the LES method over the RANS modelling is clearly demonstrated in Figs.
368 13 and 14 in capturing more detailed secondary eddies, which reflects the fundamental
369 difference of the two approaches. Essentially the RANS approach uses the time averaging
370 procedure to obtain the Reynolds averaged transport equations for the mean flow quantities and
371 all scales (both large and small) of turbulence are represented by a model such as the standard
372 k- ϵ model adapted in this paper. In contrast the LES approach employs the space filtering
373 procedure to derive the transport equations for both the mean flow quantities and the large
374 scales of turbulence, and only the smaller scale eddies that cannot be resolved by the
375 computational grid are modelled by a SGS model such as the WALE model used in the
376 comparison.

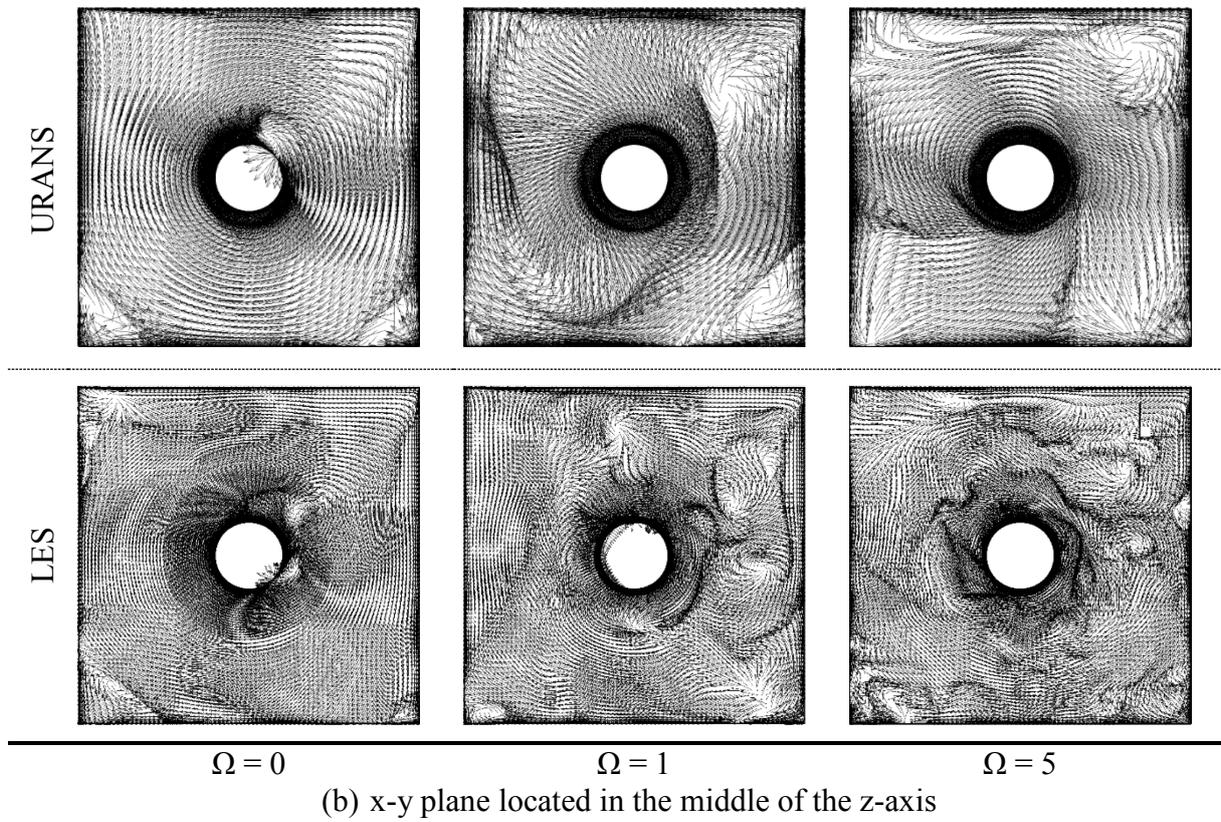
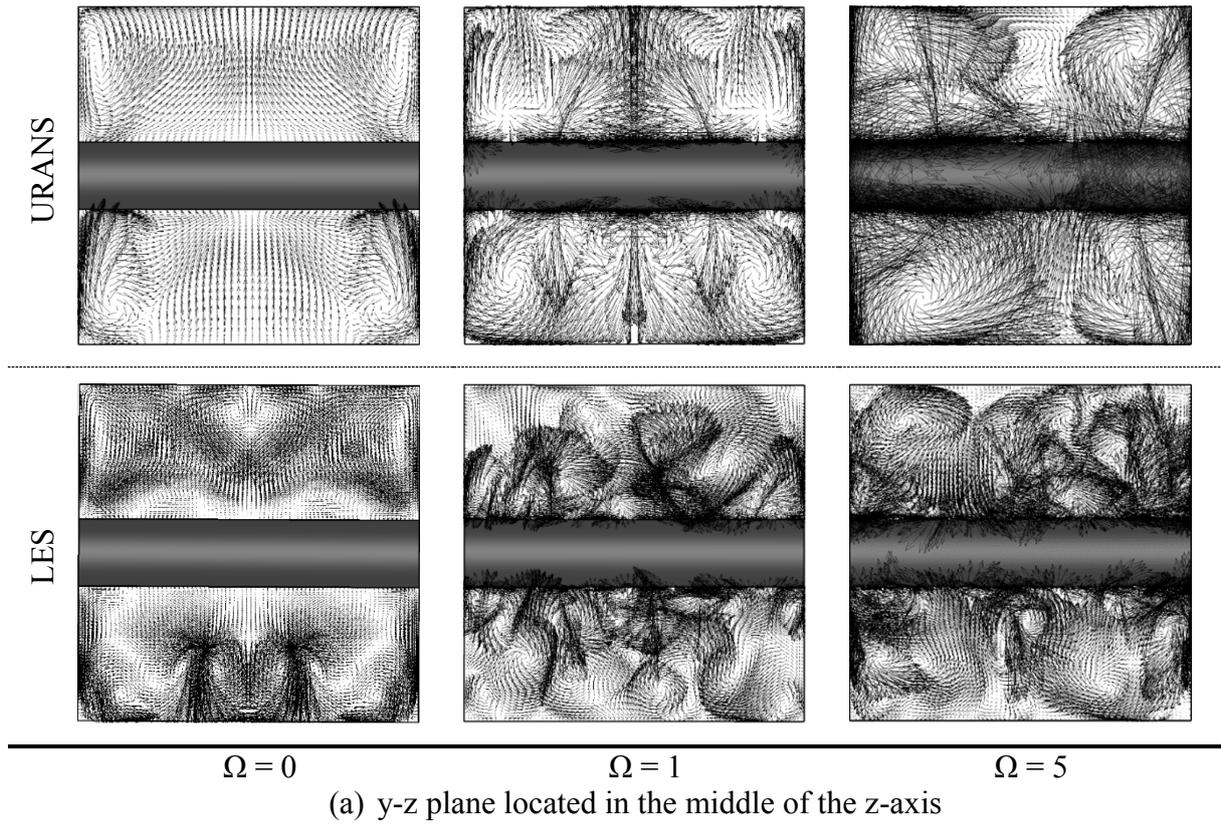


Fig. 14. Flow vectors comparison between URANS and LES at $Re = 5000$.

377 3.5.3 Nusselt number

378 Fig. 15 illustrates the comparison between the LES and URANS methods in terms of local
379 Nusselt number on the line that is located at the left of the top lid-driven wall (0, 1, 0.5 and
380 0.005, 1, 0.5) for different rotational speeds of the circular cylinder, $0 \leq \Omega \leq 5$, and at $Re =$
381 10000. For all rotational speeds, it can be clearly noticed that the LES approach shows distinct
382 advantage over the URANS approach in predicting higher heat transfer coefficients in the
383 region that is closer to the moving wall of the cavity, owing to its ability in capturing the
384 contribution from the secondary vortices.

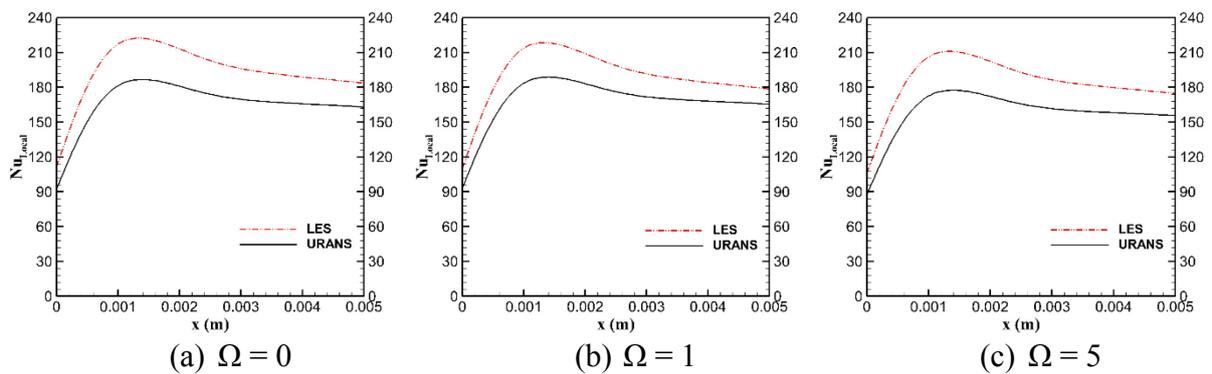


Fig. 15. Comparison of local Nusselt number for different rotational speeds and at $Re = 10000$.

385 4. Conclusions

386 The three-dimensional problem of turbulent flow within the lid-driven cubical enclosure, which
387 is differentially heated and contains a rotating cylinder, has been simulated by using the finite
388 volume method. The influences of various values of both the rotational speed of circular
389 cylinder and Reynolds number are examined, and the striking performances of the URANS and
390 LES approaches are scrutinized. The currently acquired outcomes have revealed interesting
391 behaviours of the turbulent flow and thermal fields in the obstructed enclosure, and the
392 following are the itemized observations from the present research:

- 393 • The velocity distributions and flow structures are substantially affected by the Reynolds
394 number and rotational speed of the cylinder. Increasing the rotational speed or the Reynolds
395 number commands to accretion in the average Nusselt number. The highest value of Nusselt
396 number occurs at the highest Reynolds number and rotational speed because of the high
397 increment in the fluid motion.
- 398 • For stationary cylinder, $\Omega = 0$, the flow is mainly driven by the moving top wall, and is
399 assisted by the buoyancy effect due to the temperature differences between the top and

400 bottom walls. The central main eddy (clockwise) controls most of the domain whilst the
401 secondary vortices are shown clearly at the corners of the enclosure, particularly by the LES
402 approach.

- 403 • For $\Omega = 1$, it is observed that the rotating cylinder has gained control over the regions
404 surrounding the cylinder by creating an eddy that is circumscribed about the proximity of
405 the cylinder. Many secondary vortices appear in this case because of the opposite direction
406 actions by the moving top wall and the rotational cylinder.
 - 407 • However, when the rotational speed is increased to five, it is noticed that the rotating
408 cylinder dominates more regions than the moving top wall and the buoyancy induced flow.
409 Herein, the primary vortex (anticlockwise) is led by the forced rotational movement and the
410 number of the secondary vortices is increased as a result of the increment in the flow
411 movement.
 - 412 • For all the Reynolds number values reported here, it is shown that the effects of the
413 rotational speeds, $1 \leq \Omega \leq 10$, are remarkable on the Nusselt number on the cool bottom
414 wall, but their effects on the top moving wall can be neglected unless the rotational speed
415 reaches 10.
 - 416 • In all cases of different Reynolds numbers and rotational speeds, it is demonstrated
417 convincingly that the LES method can capture more detailed secondary eddies than the
418 URANS model. Although the LES approach is more demanding in terms of computational
419 time and mesh features, this study has expounded that the LES method has distinct merits
420 over the URANS method in predicting accurately the unsteady flow structures and thermal
421 fields.
- 422

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426

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